A Research on the Effects of Braking Torque on Dynamic Load of Tractor Semi-trailer on a Straight Road with the Friction Factor

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The paper presents the research results on the dynamic load of tractor semi-trailer on a straight road with the maximum longitudinal friction factor $\Phi_{xmax} = 0.8$ at speed V0 = [60, 80]km/h, being braked with 6 different braking torques. The method of structural separation of a multi-body system is used to build a 3D dynamic model of the tractor semi-trailer and the Newton-Euler equation is used to set up the system of dynamic equations of tractor semi-trailer. MATLAB-Simulink software is used to examine the effects of braking torque on dynamic load of the tractor semi-trailer. The results showed that, the wheel force of axle 1 is increased by 200%, but the wheel force of axle 3 is reduced about 13.3%, and the wheel force of axle 6 is reduced about 21.6%. The dynamic load factor of axle 1 is increased by 200%, but the dynamic load factor of axle 3 is reduced about 9%, and the dynamic load factor of axle 6 is reduced about 22%.

Keywords: Braking torque, Dynamic load factor, Wheel force, Tractor semi-trailer.

1 Introduction

The braking torque greatly affects the braking efficiency, dynamic load, vibration and stability of tractor semi-trailer. The maximum dynamic load acting on the tractor semi-trailer is assessed by the maximum dynamic load factor ($k_{dij,max}$). The maximum dynamic load factor of the tractor semi-trailer is determined by the following formula [1, 5, 6]:

$$k_{dij,max} = \frac{F_{zij}}{F_{Gij}} = 1 + \frac{F_{CLij,max}}{F_{Gij}} ; \quad k_{dij,max} \le 2.5$$
(1)

$$F_{zij} = \begin{cases} F_{CLij} + F_{Gij} & if & h_{ij} - \left[\zeta_{Aij} - f_{ij}'\right] \ge 0\\ 0 & if & h_{ij} - \left[\zeta_{Aij} - f_{ij}'\right] \le 0 \end{cases}$$
(2)

$$F_{CLij} = \begin{cases} C_{Lij} \left(h_{ij} - \zeta_{Aij} \right) & if & h_{ij} - \left[\zeta_{Aij} - f_{ij}^{t} \right] \ge 0 \\ 0 & if & h_{ij} - \left[\zeta_{Aij} - f_{ij}^{t} \right] \le 0 \end{cases}$$
(3)

2 The three-dimensional (3D) dynamics model

The tractor semi-trailer has a very complex structure, belonging to amany objects system. Therefore, the authors used the method of structural separation of a multi-body system to build a threedimensional (3D) dynamics model of the tractor semi-trailerin the coordinate system OXYZ. The 3D dynamics model of the tractor semi-trailer is divided into three models as follows:(i) The dynamics model of the tractor semi-trailer in the OXY plane; (ii) The dynamics model of the tractor semi-trailer in the OXZ plane; (iii) The dynamics model of the tractor semi-trailer in the OYZ plane [1, 2, 3, 4].



Fig. 1. The dynamics model of the tractor semi-trailer in the OXY plane



Fig. 2. The dynamics model of the tractor semi-trailer in the OXZ plane

The Newton-Euler equation was used to set up the system of dynamic equations of the tractor semi-trailer as follows [1, 2, 3, 4, 6, 7]:

$$(m_{cl} + \sum_{I}^{3} m_{Ai}) \ddot{x}_{cl} = (F_{xIj} - F_{RIj}) \cos \delta_{Ij} - F_{yIj} \sin \delta_{Ij} - (F_{R2j} + F_{R3j}) + (F_{x2j} + F_{x3j}) - F_{wxI} - F_{kxI}$$
(4)

$$(m_{cl} + \sum_{l}^{3} m_{Ai}) \ddot{y}_{cl} = (F_{xlj} - F_{Rlj}) \sin \delta_{lj} + F_{ylj} \cos \delta_{lj} + F_{y2j} + F_{y3j} - F_{kyl} \quad (i = l \div 3)$$
(5)

$$J_{zcl}\ddot{\psi}_{cl} = [(F_{xlj} - F_{Rlj})\sin\delta_{lj} + F_{ylj}\cos\delta_{lj}]l_l + (F_{xl2} - F_{xil} + F_{Rll} - F_{Rl2})b_i - F_{yij}l_i$$

$$+ (F_{xl2}\cos\delta_{l2} - F_{xl1}\cos\delta_{l1} + F_{yl1}\sin\delta_{l1} - F_{yl2}\sin\delta_{l2} + F_{Rll}\cos\delta_{l1} - F_{Rl2}\cos\delta_{l2})b_l + F_{kyl}l_{kl}$$
(6)

$$(m_{c2} + \sum_{4}^{6} m_{Ai}) \ddot{x}_{c2} = (F_{xij} - F_{Rij}) + F_{kx2} \qquad (i = 4 \div 6)$$
⁽⁷⁾

$$(m_{c2} + \sum_{4}^{6} m_{Ai}) \ddot{y}_{c2} = F_{ky2} + F_{yij} \qquad (i = 4 \div 6)$$
(8)

$$J_{zc2}\dot{\psi}_{c2} = (F_{xi2} - F_{xi1} + F_{Ri1} - F_{Ri2})b_i - F_{yij}l_i + F_{ky2}l_{k2} \qquad (i = 4 \div 6)$$
(9)

$$m_{cl} \ddot{z}_{cl} = F_{Clj} + F_{Klj} - F_{kzl} \qquad (i = l \div 3)$$
(10)

$$J_{ycl}\ddot{\varphi}_{cl} = (F_{Cij} + F_{Kij})l_i + F_{kzl}l_{kl} - F_{kxl}(h_{cl} - h_{kl}) + M_{ij} \qquad (i = l \div 3)$$
(11)

$$m_{c2}\ddot{z}_{c2} = F_{Cij} + F_{Kij} + F_{k2} \qquad (i = 4 \div 6)$$
(12)

$$J_{yc2}\ddot{\varphi}_{c2} = -(F_{Cij} + F_{Kij})l_i + F_{kx2}(h_{c2} - h_{k2}) + F_{kz2}l_{k2} + M_{ij} \quad (i = 4 \div 6)$$
⁽¹³⁾

$$J_{xcl}\ddot{\beta}_{cl} = (F_{Cl2} + F_{Kl2} - F_{Cll} - F_{Kl1})w_l + M_{kcl} \qquad (i = l \div 3)$$
(14)

$$J_{xc2}\ddot{\beta}_{c2} = (F_{Ci2} + F_{Ki2} - F_{Cil} - F_{Kil})w_i - M_{kx2} \qquad (i = l \div 3)$$
(15)

$$J_{Axi}\ddot{\beta}_{Ai} = (F_{Cil} + F_{Kil} - F_{Ci2} - F_{Ki2})w_i + (F_{CLi2} + F_{KLi2} - F_{CLil} - F_{KLil})b_i - F_{yij}(r_{ij} + \xi_{Aij}) \quad (i = 1 \div 6)$$
(16)

$$m_{Ai}(\ddot{z}_{Ai} + \dot{\beta}_{Ai} \dot{y}_{Ai}) = F_{CLij} + F_{KLij} - F_{Cij} - F_{Kij} \qquad (i = l \div 6)$$
(17)

$$m_{Ai}(\ddot{y}_{Ai} - \dot{\beta}_{Ai}\dot{z}_{Ai}) = F_i + F_{vii} \qquad (i = 1 \div 6)$$
(18)

$$J_{Axij}\ddot{\varphi}_{ij} = M_{Aij} - M_{Bij} - F_{xij}r_{dij} \qquad (i = l \div 6)$$
⁽¹⁹⁾

3 Survey results and discussions

Matlab-simulink software was used to test the effects of braking torque on dynamic load of tractor semi-trailer. The tractor semi-trailer is moved on a straight road with the maximum longitudinal friction factor $\phi_{xmax} = 0.8$ at speeds $V_o = [60, 80]$ km/h. The tractor semi-trailer is braked with 6 braking torques $M_B = [0.5, 0.6, 0.7, 0.8, 0.9, 1] M_{Bmax}$ (with $M_{Bmax} = F_G \phi_{xmax} r_{dyn}$).



Fig. 3. The driving torque and braking torque

The input driving and braking torques of the survey model are shown in Figure 3, line 1 is $M_B=0.5M_{Bmax}$; line 2 is $M_B=0.6M_{Bmax}$; line 3 is $M_B=0.7M_{Bmax}$; line 4 is $M_B=0.8M_{Bmax}$; line 5 is $M_B=0.9M_{Bmax}$; line 6 is $M_B=M_{Bmax}$.



Fig. 4. The wheel load on axle1



Fig. 5. The wheel load on axle 3

Figure (4, 5, 6) are the graphs of wheel load (F_{zij}) of the axle (1, 3, 6). From the graphs we see that, when the tractor semi-trailer is moved on a straight road with $\phi_{xmax}=0.8$ at speeds $V_0=[60, 80]$ km/h and then it is braked with 6 braking torques $M_B=[0.5, 0.6, 0.7, 0.8, 0.9, 1]M_{Bmax}$, the wheel force of axle 1 is increased, but the wheel force of axle 3 and the wheel force of axle 6 are decreased,

$$F_{Z11} = (2.8 \div 5.6) kN; F_{Z31} = (4.15 \div 3.6) kN; F_{Z61} = (3.98 \div 3.12) kN,$$

The graphs of dynamic load factor of the tractor semi-trailer (k_{dij}) are shown as figures (7, 8, 9). When the tractor semi-trailer is moved on a straight road with ϕ_{xmax} =0.8 at speeds V₀=[60, 80]km/h and then it is braked with 6 braking torques M_B=[0.5, 0.6, 0.7, 0.8, 0.9, 1]M_{Bmax}, the dynamic load factor of axle 1 is increased, but the dynamic load factor of axle 3 and the dynamic load factor of axle 6 are decreased,

$$k_{d11} = (1.0 \div 2.0); k_{d31} = (1.0 \div 0.91); k_{d61} = (1.0 \div 0.78).$$



Fig. 6. The wheel load on axle 6



Fig. 7. The dynamic load factor of the front axle



Fig. 8. The dynamic load factor of the middle axle



DO THI K_{d31} 1.15 . 2 1.1 - 3 - 4 - 5 1.05 6 k d31 0.95 0.9 2 4 t(s) 6 8

b. $V_0 = 80 \text{ km/h}$



Fig. 9. The dynamic load factor of the rear axle

4 Conclusion

When the tractor semi-trailer is moved on a straight road with ϕ_{xmax} =0.8 at speeds V₀=[60, 80]km/h and then it is braked with 6 braking torques M_B=[0.5, 0.6, 0.7, 0.8, 0.9, 1]M_{Bmax}. The wheel force of axle 1 is increased by 200%, but the wheel force of axle 3 is reduced about 13.3%, and the wheel force of axle 6 is reduced about 21.6%.

The dynamic load factor of axle 1 is increased by 200%, but the dynamic load factor of axle 3 is reduced about 9%, and the dynamic load factor of axle 6 is reduced about 22%.

References

- Tung, N. T. (2017). Research on braking efficiency on the roads with different grip coefficients of the tractor semi-trailer and proposed measures to reduce traffic accidents. *Doctoral thesis, Hanoi University of Science* and Technology, Vietnam.
- [2] Tung, N. T., Huong, V. V. and Kiet, P. T. (2020). Experimental research on determining the vertical tyre force of a tractor semi-trailer. *International Journal of Modern Physics B, Singapore*, 2040163-1 - 2040163-7.
- [3] Tung, N. T. and Huong, V. V. (2020). The effect of the wheel rotation angle on the braking efficiency of the tractor semi-trailer on the wet roundabout route. *Lecture notes in networks and systems, Springer Switzerland*, 798–804.
- [4] Tung, N. T. et al. (2021). A survey on the effects of bumpy road on the vibration of multi-purpose forest fire fighting vehicle. *Engineering solid mechanic*, 1-8.
- [5] Tung, N. T. et al. (2021). Assessment breaking streng the chassis of multi-purpose forest fire fighting vehicle. IOP conference series: Materials science and engineering, 1-7.
- [6] Tung, N. T. and Huong, V. V. (2021). Research on the dynamic load of the tractor semi-trailer when braking on the round road. *Lecture notes in mechanical engineering*, United States Springer Verlag, 456-461.
- [7] Tung, N. T. (2021). Setting up the braking force measurement system of the tractor semi-trailer. *Engineering* solid mechanic, 1-10.